

AD-A156 774

AQUATIC PLANT CONTROL RESEARCH PROGRAM A MATHEMATICAL  
MODEL OF SUBMERSED... (U) RENSSELAER POLYTECHNIC INST  
TROY NY CENTER FOR ECOLOGICAL MOD... C D COLLINS ET AL.  
MAY 85 WES/MP/A-85-2 DACW39-81-C-0036

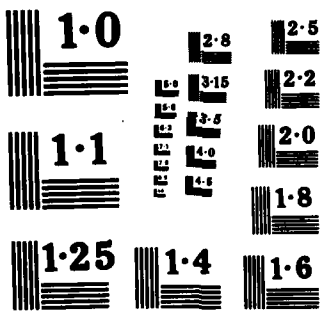
1/8

UNCLASSIFIED

F/G 8/8

NL

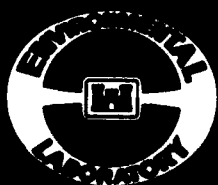
1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11  
12  
13  
14  
15  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60  
61  
62  
63  
64  
65  
66  
67  
68  
69  
70  
71  
72  
73  
74  
75  
76  
77  
78  
79  
80  
81  
82  
83  
84  
85  
86  
87  
88  
89  
90  
91  
92  
93  
94  
95  
96  
97  
98  
99  
100  
101  
102  
103  
104  
105  
106  
107  
108  
109  
110  
111  
112  
113  
114  
115  
116  
117  
118  
119  
120  
121  
122  
123  
124  
125  
126  
127  
128  
129  
130  
131  
132  
133  
134  
135  
136  
137  
138  
139  
140  
141  
142  
143  
144  
145  
146  
147  
148  
149  
150  
151  
152  
153  
154  
155  
156  
157  
158  
159  
160  
161  
162  
163  
164  
165  
166  
167  
168  
169  
170  
171  
172  
173  
174  
175  
176  
177  
178  
179  
180  
181  
182  
183  
184  
185  
186  
187  
188  
189  
190  
191  
192  
193  
194  
195  
196  
197  
198  
199  
200  
201  
202  
203  
204  
205  
206  
207  
208  
209  
210  
211  
212  
213  
214  
215  
216  
217  
218  
219  
220  
221  
222  
223  
224  
225  
226  
227  
228  
229  
230  
231  
232  
233  
234  
235  
236  
237  
238  
239  
240  
241  
242  
243  
244  
245  
246  
247  
248  
249  
250  
251  
252  
253  
254  
255  
256  
257  
258  
259  
260  
261  
262  
263  
264  
265  
266  
267  
268  
269  
270  
271  
272  
273  
274  
275  
276  
277  
278  
279  
280  
281  
282  
283  
284  
285  
286  
287  
288  
289  
290  
291  
292  
293  
294  
295  
296  
297  
298  
299  
300  
301  
302  
303  
304  
305  
306  
307  
308  
309  
310  
311  
312  
313  
314  
315  
316  
317  
318  
319  
320  
321  
322  
323  
324  
325  
326  
327  
328  
329  
330  
331  
332  
333  
334  
335  
336  
337  
338  
339  
340  
341  
342  
343  
344  
345  
346  
347  
348  
349  
350  
351  
352  
353  
354  
355  
356  
357  
358  
359  
360  
361  
362  
363  
364  
365  
366  
367  
368  
369  
370  
371  
372  
373  
374  
375  
376  
377  
378  
379  
380  
381  
382  
383  
384  
385  
386  
387  
388  
389  
390  
391  
392  
393  
394  
395  
396  
397  
398  
399  
400  
401  
402  
403  
404  
405  
406  
407  
408  
409  
410  
411  
412  
413  
414  
415  
416  
417  
418  
419  
420  
421  
422  
423  
424  
425  
426  
427  
428  
429  
430  
431  
432  
433  
434  
435  
436  
437  
438  
439  
440  
441  
442  
443  
444  
445  
446  
447  
448  
449  
450  
451  
452  
453  
454  
455  
456  
457  
458  
459  
460  
461  
462  
463  
464  
465  
466  
467  
468  
469  
470  
471  
472  
473  
474  
475  
476  
477  
478  
479  
480  
481  
482  
483  
484  
485  
486  
487  
488  
489  
490  
491  
492  
493  
494  
495  
496  
497  
498  
499  
500  
501  
502  
503  
504  
505  
506  
507  
508  
509  
510  
511  
512  
513  
514  
515  
516  
517  
518  
519  
520  
521  
522  
523  
524  
525  
526  
527  
528  
529  
530  
531  
532  
533  
534  
535  
536  
537  
538  
539  
540  
541  
542  
543  
544  
545  
546  
547  
548  
549  
550  
551  
552  
553  
554  
555  
556  
557  
558  
559  
560  
561  
562  
563  
564  
565  
566  
567  
568  
569  
570  
571  
572  
573  
574  
575  
576  
577  
578  
579  
580  
581  
582  
583  
584  
585  
586  
587  
588  
589  
590  
591  
592  
593  
594  
595  
596  
597  
598  
599  
600  
601  
602  
603  
604  
605  
606  
607  
608  
609  
610  
611  
612  
613  
614  
615  
616  
617  
618  
619  
620  
621  
622  
623  
624  
625  
626  
627  
628  
629  
630  
631  
632  
633  
634  
635  
636  
637  
638  
639  
640  
641  
642  
643  
644  
645  
646  
647  
648  
649  
650  
651  
652  
653  
654  
655  
656  
657  
658  
659  
660  
661  
662  
663  
664  
665  
666  
667  
668  
669  
670  
671  
672  
673  
674  
675  
676  
677  
678  
679  
680  
681  
682  
683  
684  
685  
686  
687  
688  
689  
690  
691  
692  
693  
694  
695  
696  
697  
698  
699  
700  
701  
702  
703  
704  
705  
706  
707  
708  
709  
710  
711  
712  
713  
714  
715  
716  
717  
718  
719  
720  
721  
722  
723  
724  
725  
726  
727  
728  
729  
730  
731  
732  
733  
734  
735  
736  
737  
738  
739  
740  
741  
742  
743  
744  
745  
746  
747  
748  
749  
750  
751  
752  
753  
754  
755  
756  
757  
758  
759  
760  
761  
762  
763  
764  
765  
766  
767  
768  
769  
770  
771  
772  
773  
774  
775  
776  
777  
778  
779  
780  
781  
782  
783  
784  
785  
786  
787  
788  
789  
790  
791  
792  
793  
794  
795  
796  
797  
798  
799  
800  
801  
802  
803  
804  
805  
806  
807  
808  
809  
810  
811  
812  
813  
814  
815  
816  
817  
818  
819  
820  
821  
822  
823  
824  
825  
826  
827  
828  
829  
830  
831  
832  
833  
834  
835  
836  
837  
838  
839  
840  
841  
842  
843  
844  
845  
846  
847  
848  
849  
850  
851  
852  
853  
854  
855  
856  
857  
858  
859  
860  
861  
862  
863  
864  
865  
866  
867  
868  
869  
870  
871  
872  
873  
874  
875  
876  
877  
878  
879  
880  
881  
882  
883  
884  
885  
886  
887  
888  
889  
890  
891  
892  
893  
894  
895  
896  
897  
898  
899  
900  
901  
902  
903  
904  
905  
906  
907  
908  
909  
910  
911  
912  
913  
914  
915  
916  
917  
918  
919  
920  
921  
922  
923  
924  
925  
926  
927  
928  
929  
930  
931  
932  
933  
934  
935  
936  
937  
938  
939  
940  
941  
942  
943  
944  
945  
946  
947  
948  
949  
950  
951  
952  
953  
954  
955  
956  
957  
958  
959  
960  
961  
962  
963  
964  
965  
966  
967  
968  
969  
970  
971  
972  
973  
974  
975  
976  
977  
978  
979  
980  
981  
982  
983  
984  
985  
986  
987  
988  
989  
990  
991  
992  
993  
994  
995  
996  
997  
998  
999  
1000  
1001  
1002  
1003  
1004  
1005  
1006  
1007  
1008  
1009  
1010  
1011  
1012  
1013  
1014  
1015  
1016  
1017  
1018  
1019  
1020  
1021  
1022  
1023  
1024  
1025  
1026  
1027  
1028  
1029  
1030  
1031  
1032  
1033  
1034  
1035  
1036  
1037  
1038  
1039  
1040  
1041  
1042  
1043  
1044  
1045  
1046  
1047  
1048  
1049  
1050  
1051  
1052  
1053  
1054  
1055  
1056  
1057  
1058  
1059  
1060  
1061  
1062  
1063  
1064  
1065  
1066  
1067  
1068  
1069  
1070  
1071  
1072  
1073  
1074  
1075  
1076  
1077  
1078  
1079  
1080  
1081  
1082  
1083  
1084  
1085  
1086  
1087  
1088  
1089  
1090  
1091  
1092  
1093  
1094  
1095  
1096  
1097  
1098  
1099  
1100  
1101  
1102  
1103  
1104  
1105  
1106  
1107  
1108  
1109  
1110  
1111  
1112  
1113  
1114  
1115  
1116  
1117  
1118  
1119  
1120  
1121  
1122  
1123  
1124  
1125  
1126  
1127  
1128  
1129  
1130  
1131  
1132  
1133  
1134  
1135  
1136  
1137  
1138  
1139  
1140  
1141  
1142  
1143  
1144  
1145  
1146  
1147  
1148  
1149  
1150  
1151  
1152  
1153  
1154  
1155  
1156  
1157  
1158  
1159  
1160  
1161  
1162  
1163  
1164  
1165  
1166  
1167  
1168  
1169  
1170  
1171  
1172  
1173  
1174  
1175  
1176  
1177  
1178  
1179  
1180  
1181  
1182  
1183  
1184  
1185  
1186  
1187  
1188  
1189  
1190  
1191  
1192  
1193  
1194  
1195  
1196  
1197  
1198  
1199  
1200  
1201  
1202  
1203  
1204  
1205  
1206  
1207  
1208  
1209  
1210  
1211  
1212  
1213  
1214  
1215  
1216  
1217  
1218  
1219  
1220  
1221  
1222  
1223  
1224  
1225  
1226  
1227  
1228  
1229  
1230  
1231  
1232  
1233  
1234  
1235  
1236  
1237  
1238  
1239  
1240  
1241  
1242  
1243  
1244  
1245  
1246  
1247  
1248  
1249  
1250  
1251  
1252  
1253  
1254  
1255  
1256  
1257  
1258  
1259  
1260  
1261  
1262  
1263  
1264  
1265  
1266  
1267  
1268  
1269  
1270  
1271  
1272  
1273  
1274  
1275  
1276  
1277  
1278  
1279  
1280  
1281  
1282  
1283  
1284  
1285  
1286  
1287  
1288  
1289  
1290  
1291  
1292  
1293  
1294  
1295  
1296  
1297  
1298  
1299  
1300  
1301  
1302  
1303  
1304  
1305  
1306  
1307  
1308  
1309  
1310  
1311  
1312  
1313  
1314  
1315  
1316  
1317  
1318  
1319  
1320  
1321  
1322  
1323  
1324  
1325  
1326  
1327  
1328  
1329  
1330  
1331  
1332  
1333  
1334  
1335  
1336  
1337  
1338  
1339  
1340  
1341  
1342  
1343  
1344  
1345  
1346  
1347  
1348  
1349  
1350  
1351  
1352  
1353  
1354  
1355  
1356  
1357  
1358  
1359  
1360  
1361  
1362  
1363  
1364  
1365  
1366  
1367  
1368  
1369  
1370  
1371  
1372  
1373  
1374  
1375  
1376  
1377  
1378  
1379  
1380  
1381  
1382  
1383  
1384  
1385  
1386  
1387  
1388  
1389  
1390  
1391  
1392  
1393  
1394  
1395  
1396  
1397  
1398  
1399  
1400  
1401  
1402  
1403  
1404  
1405  
1406  
1407  
1408  
1409  
1410  
1411  
1412  
1413  
1414  
1415  
1416  
1417  
1418  
1419  
1420  
1421  
1422  
1423  
1424  
1425  
1426  
1427  
1428  
1429  
1430  
1431  
1432  
1433  
1434  
1435  
1436  
1437  
1438  
1439  
1440  
1441  
1442  
1443  
1444  
1445  
1446  
1447  
1448  
1449  
1450  
1451  
1452  
1453  
1454  
1455  
1456  
1457  
1458  
1459  
1460  
1461  
1462  
1463  
1464  
1465  
1466  
1467  
1468  
1469  
1470  
1471  
1472  
1473  
1474  
1475  
1476  
1477  
1478  
1479  
1480  
1481  
1482  
1483  
1484  
1485  
1486  
1487  
1488  
1489  
1490  
1491  
1492  
1493  
1494  
1495  
1496  
1497  
1498  
1499  
1500  
1501  
1502  
1503  
1504  
1505  
1506  
1507  
1508  
1509  
1510  
1511  
1512  
1513  
1514  
1515  
1516  
1517  
1518  
1519  
1520  
1521  
1522  
1523  
1524  
1525  
1526  
1527  
1528  
1529  
1530  
1531  
1532  
1533  
1534  
1535  
1536  
1537  
1538  
1539  
1540  
1541  
1542  
1543  
1544  
1545  
1546  
1547  
1548  
1549  
1550  
1551  
1552  
1553  
1554  
1555  
1556  
1557  
1558  
1559  
1560  
1561  
1562  
1563  
1564  
1565  
1566  
1567  
1568  
1569  
1570  
1571  
1572  
1573  
1574  
1575  
1576  
1577  
1578  
1579  
1580  
1581  
1582  
1583  
1584  
1585  
1586  
1587  
1588  
1589  
1590  
1591  
1592  
1593  
1594  
1595  
1596  
1597  
1598  
1599  
1600  
1601  
1602  
1603  
1604  
1605  
1606  
1607  
1608  
1609  
1610  
1611  
1612  
1613  
1614  
1615  
1616  
1617  
1618  
1619  
1620  
1621  
1622  
1623  
1624  
1625  
1626  
1627  
1628  
1629  
1630  
1631  
1632  
1633  
1634  
1635  
1636  
1637  
1638  
1639  
1640  
1641  
1642  
1643  
1644  
1645  
1646  
1647  
1648  
1649  
1650  
1651  
1652  
1653  
1654  
1655  
1656  
1657  
1658  
1659  
1660  
1661  
1662  
1663  
1664  
1665  
1666  
1667  
1668  
1669  
1670  
1671  
1672  
1673  
1674  
1675  
1676  
1677  
1678  
1679  
1680  
1681  
1682  
1683  
1684  
1685  
1686  
1687  
1688  
1689  
1690  
1691  
1692  
1693  
1694  
1695  
1696  
1697  
1698  
1699  
1700  
1701  
1702  
1703  
1704  
1705  
1706  
1707  
1708  
1709  
1710  
1711  
1712  
1713  
1714  
1715  
1716  
1717  
1718  
1719  
1720  
1721  
1722  
1723  
1724  
1725  
1726  
1727  
1728  
1729  
1730  
1731  
1732  
1733  
1734  
1735  
1736  
1737  
1738  
1739  
1740  
1741  
1742  
1743  
1744  
1745  
1746  
1747  
1748  
1749  
1750  
1751  
1752  
1753  
1754  
1755  
1756  
1757  
1758  
1759  
1760  
1761  
1762  
1763  
1764  
1765  
1766  
1767  
1768  
1769  
1770  
1771  
1772  
1773  
1774  
1775  
1776  
1777  
1778  
1779  
1780  
1781  
1782  
1783  
1784  
1785  
1786  
1787  
1788  
1789  
1790  
1791  
1792  
1793  
1794  
1795  
1796  
1797  
1798  
1799  
1800  
1801  
1802  
1803  
1804  
1805  
1806  
1807  
1808  
1809  
1810  
1811  
1812  
1813  
1814  
1815  
1816  
1817  
1818  
1819  
1820  
1821  
1822  
1823  
1824  
1825  
1826  
1827  
1828  
1829  
1830  
1831  
1832  
1833  
1834  
1835  
1836  
1837  
1838  
1839  
1840  
1841  
1842  
1843  
1844  
1845  
1846  
1847  
1848  
1849  
1850  
1851  
1852  
1853  
1854  
1855  
1856  
1857  
1858  
1859  
1860  
1861  
1862  
1863  
1864  
1865  
1866  
1867  
1868  
1869  
1870  
1871  
1872  
1873  
1874  
1875  
1876  
1877  
1878  
1879  
1880  
1881  
1882  
1883  
1884  
1885  
1886  
1887  
1888  
1889  
1890  
1891  
1892  
1893  
1894  
1895  
1896  
1897  
1898  
1899  
1900  
1901  
1902  
1903  
1904  
1905  
1906  
1907  
1908  
1909  
1910  
1911  
1912  
1913  
1914  
1915  
1916  
1917  
1918  
1919  
1920  
1921  
1922  
1923  
1924  
1925  
1926  
1927  
1928  
1929  
1930  
1931  
1932  
1933  
1934  
1935  
1936  
1937  
1938  
1939  
1940  
1941  
1942  
1943  
1944  
1945  
1946  
1947  
1948  
1949  
1950  
1951  
1952  
1953  
1954  
1955  
1956  
1957  
1958  
1959  
1960  
1961  
1962  
1963  
1964  
1965  
1966  
1967  
1968  
1969  
1970  
1971  
1972  
1973  
1974  
1975  
1976  
1977  
1978  
1979  
1980  
1981  
1982  
1983  
1984  
1985  
1986  
1987  
1988  
1989  
1990  
1991  
1992  
1993  
1994  
1995  
1996  
1997  
1998  
1999  
2000  
2001  
2002  
2003  
2004  
2005  
2006  
2007  
2008  
2009  
2010  
2011  
2012  
2013  
2014  
2015  
2016  
2017  
2018  
2019  
2020  
2021  
2022  
2023  
2024  
2025  
2026  
2027  
2028  
2029  
2030  
2031  
2032  
2033  
2034  
2035  
2036  
2037  
2038  
2039  
2040  
2041  
2042  
2043  
2044  
2045  
2046  
2047  
2048  
2049  
2050  
2051  
2052  
2053  
2054  
2055  
2056  
2057  
2058  
2059  
2060  
2061  
2062  
2063  
2064  
2065  
2066  
2067  
2068  
2069  
2070  
2071  
2072  
2073  
2074  
2075  
2076  
2077  
2078  
2079  
2080  
2081  
2082  
2083  
2084  
2085  
2086  
2087  
2088  
2089  
2090  
2091  
2092  
2093  
2094  
2095  
2096  
2097  
2098  
2099  
2100  
2101  
2102  
2103  
2104  
2105  
2106  
2107  
2108  
2109  
2110  
2111  
2112  
2113  
2114  
2115  
2116  
2117  
2118  
2119  
2120  
2121  
2122  
2123  
2124  
2125  
2126  
2127  
2128  
2129  
2130  
2131  
2132  
2133  
2134  
2135  
2136  
2137  
2138  
2139  
2140  
2141  
2142  
2143  
2144  
2145  
2146  
2147  
2148  
2149  
2150  
2151  
2152  
2153  
2154  
2155  
2156  
2157  
2158  
2159  
2160  
2161  
2162  
2163  
2164  
2165  
2166  
2167  
2168  
2169  
2170  
2171  
2172  
2173  
2174  
2175  
2176  
2177  
2178  
2179  
2180  
2181  
2182  
2183  
2184  
2185  
2186  
2187  
2188  
2189  
2190  
2191  
2192  
2193  
2194





US Army Corps  
of Engineers

AD-A156 774



**AQUATIC PLANT CONTROL  
RESEARCH PROGRAM**

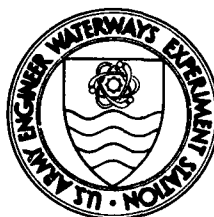
MISCELLANEOUS PAPER A-85-2

**A MATHEMATICAL MODEL OF  
SUBMERSED AQUATIC PLANTS**

by

Carol Desormeau Collins, Richard A. Park, Charles W. Boylen

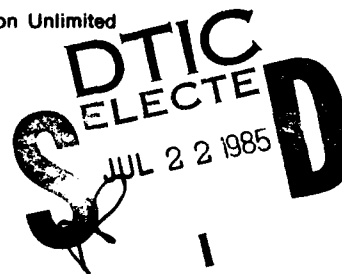
Center for Ecological Modeling  
Rensselaer Polytechnic Institute  
Troy, New York 12181



May 1985

Final Report

Approved For Public Release; Distribution Unlimited



DTIC FILE COPY

Prepared for DEPARTMENT OF THE ARMY  
US Army Corps of Engineers  
Washington, DC 20314-1000

Under Contract No. DACW39-81-C-0036

Monitored by Environmental Laboratory  
US Army Engineer Waterways Experiment Station  
PO Box 631, Vicksburg, Mississippi 39180-0631

85 07 09 02 5

Destroy this report when no longer needed. Do not return  
it to the originator.

The findings in this report are not to be construed as an official  
Department of the Army position unless so designated  
by other authorized documents.

The contents of this report are not to be used for  
advertising, publication, or promotional purposes.  
Citation of trade names does not constitute an  
official endorsement or approval of the use of  
such commercial products.

Unclassified

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER Miscellaneous Paper A-85-2	2. GOVT ACCESSION NO. AD-A156 074	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) A MATHEMATICAL MODEL OF SUBMERSED AQUATIC PLANTS	5. TYPE OF REPORT & PERIOD COVERED Final report	
7. AUTHOR(s) Carol Desormeau Collins, Richard A. Park, Charles W. Boylen	6. PERFORMING ORG. REPORT NUMBER	
9. PERFORMING ORGANIZATION NAME AND ADDRESS Rensselaer Polytechnic Institute Center for Ecological Modeling Troy, New York 12181	8. CONTRACT OR GRANT NUMBER(s) Contract No. DACW39-81-C-0036	
11. CONTROLLING OFFICE NAME AND ADDRESS DEPARTMENT OF THE ARMY US Army Corps of Engineers Washington, DC 20314-1000	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS Aquatic Plant Control Research Program	
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office) US Army Engineer Waterways Experiment Station Environmental Laboratory PO Box 631, Vicksburg, Mississippi 39180-0631	12. REPORT DATE May 1985	
	13. NUMBER OF PAGES 37	
	15. SECURITY CLASS. (of this report) Unclassified	
16. DISTRIBUTION STATEMENT (of this Report)  Approved for public release; distribution unlimited.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES  Available from National Technical Information Service, 5285 Port Royal Road, Springfield, Virginia 22161.		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Aquatic ecology; (LC) Aquatic plants--Mathematical models; (LC) <del>GE-QUAL-R1</del> (WES) Eurasian watermilfoil; (LC) and Hydrilla (LC) → Water quality management, (LC)		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) → Submersed aquatic plants or macrophytes often contribute significantly to primary production in lakes and reservoirs. Macrophyte growth and decomposi- tion can influence the physical, chemical, and biological characteristics of aquatic ecosystems, including temperature and concentrations of dissolved oxy- gen, nitrogen, phosphorus, inorganic carbon, detritus, phytoplankton, and fish.		

(Continued)

DD FORM 1 JAN 73 1473 EDITION OF 1 NOV 65 IS OBSOLETE

Unclassified

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

Unclassified

SECURITY CLASSIFICATION OF THIS PAGE(When Data Entered)

20. ABSTRACT (Continued).

A mathematical model of submersed aquatic macrophyte growth and decomposition was developed for use with the US Army Corps of Engineers' one-dimensional reservoir water quality model, CE-QUAL-R1, which was developed under the Environmental and Water Quality Operational Studies (EWQOS). The ecological processes recommended for inclusion with the macrophyte compartment include gross production, dark respiration, photorespiration, nonpredatory mortality, and grazing. The influence of these processes on other compartments in CE-QUAL-R1 is described.

Select process equations have been validated using a stand-alone version of the recommended model based upon experimental results derived from the literature and other research at the US Army Engineer Waterways Experiment Station for two macrophyte species, *Myriophyllum spicatum* and *Hydrilla verticillata*. Management control strategies can be simulated for mechanical harvesting and chemical control of the plants. *Remarks:*

Accession For	
NTIS GRA&I	<input checked="checked" type="checkbox"/>
DTIC TAB	<input type="checkbox"/>
Unannounced	<input type="checkbox"/>
Justification	
Pr	
Distribution/	
Availability Codes	
Dist	Avail and/or Special
A-1	

Unclassified

SECURITY CLASSIFICATION OF THIS PAGE(When Data Entered)

## Preface

This investigation was supported by the Aquatic Plant Control Research Program (APCRP), sponsored by the Office, Chief of Engineers (OCE), and was managed by the US Army Engineer Waterways Experiment Station (WES), Vicksburg, Miss. The OCE Technical Monitor was Mr. E. Carl Brown.

This is the final report for Contract No. DACW39-81-C-0036, "A Mathematical Model of Submersed Aquatic Plants," prepared by Rensselaer Polytechnic Institute (RPI), Troy, N. Y. Authors of this report were Drs. Carol Desormeau Collins, Richard A. Park, and Charles W. Boylen, RPI. The model was conceptualized and developed for incorporation into the US Army Corps of Engineers' reservoir water quality model, CE-QUAL-R1, which was developed during the conduct of the Environmental and Water Quality Operational Studies (EWQOS). CE-QUAL-R1 is a numerical, one-dimensional model that describes the vertical distribution of thermal energy and biological and chemical materials in a reservoir through time. The mathematical structure of the model is based on horizontal layers; temperature and materials concentration gradients are computed only in the vertical direction.

The original contract called for the development of algorithms and the programming of those algorithms for inclusion in CE-QUAL-R1. However, in subsequent discussions with the contract officer at the time, Mr. Joseph Norton, Environmental Research and Simulation Division (ERSD), and with other staff of the WES, Environmental Laboratory (EL), including Drs. Joseph H. Wlosinski and Allan S. Lessem, it was agreed that the programming should be done by the Environmental Laboratory staff most familiar with CE-QUAL-R1. The draft report was reviewed by Drs. Wlosinski and Lessem and Messrs. Mark S. Dortch and Jack B. Waide.

Manager of the APCRP was Mr. J. Lewis Decell. General supervision was provided by Mr. Donald L. Robey, Chief, ERSD. Chief of the EL during the conduct of this investigation was Dr. John Harrison.

Commanders and Directors of WES during the study and preparation of the report were COL Tilford C. Creel, CE, and COL Robert C. Lee, CE. Technical Director was Mr. F. R. Brown.

This report should be cited as follows:

Collins, C. D., Park, R. A., and Boylen, C. W. 1985. "A Mathematical Model of Submersed Aquatic Plants," Miscellaneous Paper A-85-2, prepared by Rensselaer Polytechnic Institute, Troy, N. Y., for the US Army Engineer Waterways Experiment Station, Vicksburg, Miss.



# Contents

	<u>Page</u>
Preface . . . . .	1
Introduction . . . . .	4
Background . . . . .	4
Report composition . . . . .	6
Recommended Physiologic Processes . . . . .	6
Macrophyte processes . . . . .	7
Interactions with other compartments in CE-QUAL-R1 . . . . .	11
Spatial Relationships . . . . .	12
Management Control Processes . . . . .	15
Process Validation . . . . .	16
Recommendations . . . . .	19
References . . . . .	19
Appendix A: Macrophyte Model Stand-Alone Version . . . . .	A1
Introduction . . . . .	A1
State Variable Equations . . . . .	A2
Process Equations . . . . .	A3
Appendix B: Macrophyte Model Parameter List . . . . .	B1

## A MATHEMATICAL MODEL OF SUBMERSED AQUATIC PLANTS

7

### Introduction

#### Background

1. Submersed aquatic plants or macrophytes often contribute significantly to the productivity of lakes and reservoirs. Macrophytes can become so abundant that they become a nuisance to recreational and navigational activities. Their growth and decomposition also influence other biotic and abiotic components of the ecosystem. The littoral community of many eutrophic systems is often dominated by a single species of macrophyte. Under less eutrophic conditions, several species may coexist. The growth of aquatic plants is controlled by many factors, including (a) growth properties of the plant; (b) physical factors such as temperature, irradiance levels, and changes in water elevation; and (c) physiological characteristics of the plant such as nutrient requirements, photoadaptation, and sediment preference.

2. The importance of macrophytes to the aquatic ecosystem necessitated the development and incorporation of a macrophyte submodel in the US Army Corps of Engineers' one-dimensional reservoir water quality model, CE-QUAL-R1 (Environmental Laboratory 1982), which was developed during the conduct of the Environmental and Water Quality Operational Studies (EWQOS). This report describes the development and formulation of this macrophyte submodel for inclusion in CE-QUAL-R1. The model simulates growth and decomposition of macrophytes. The influence of the plants on other compartments in CE-QUAL-R1 is also included in the model.

3. To make the proposed submodel complementary with CE-QUAL-R1, the following recommendations are made regarding the computation and layering scheme of CE-QUAL-R1. Macrophytes should be regarded as occupying the bottom surface of each layer in the reservoir within the euphotic zone. As such, they are not subject to advection or diffusion and are not transported in inflowing or outflowing waters. The macrophyte compartment should have units of grams per layer. As the layers are resized in CE-QUAL-R1, dependent on the balance of inflowing and outflowing waters, the macrophyte biomass should be reapportioned to reflect the appropriate densities for those layers. If the surface elevation drops, macrophytes in the dewatered zone should no longer be included in the computation. If the water surface elevation increases and

inundates new areas, the macrophyte density in the new area should be given a small "seed" value to represent colonization.

4. Irradiance reaching a particular model layer determines the plants' growth response. Changes in water level can affect irradiance at a particular level. Drawdown may suddenly expose submersed plants to higher irradiances as the depth of water through which light is transmitted decreases. Conversely, an increase in reservoir pool elevation may result in greater light attenuation. Light attenuation for a particular layer in CE-QUAL-R1 is dependent upon the extinction coefficient of water and on shading by suspended solids, detritus, zooplankton, and phytoplankton. It is recommended that self-shading for macrophytes also be included in the model.

5. The following processes are recommended for inclusion in the macrophyte model: gross production, dark respiration, photorespiration, nonpredatory mortality, and grazing. Control measures affecting macrophytes, such as mechanical harvesting and herbicidal treatment, should also be included in the model as described in this report. Decomposition processes already modeled in CE-QUAL-R1 would be affected by macrophyte contributions to existing detritus and sediment compartments. A flow diagram of the interactions of the new macrophyte compartment with other model compartments summarizes the proposed changes to CE-QUAL-R1 (Figure 1).

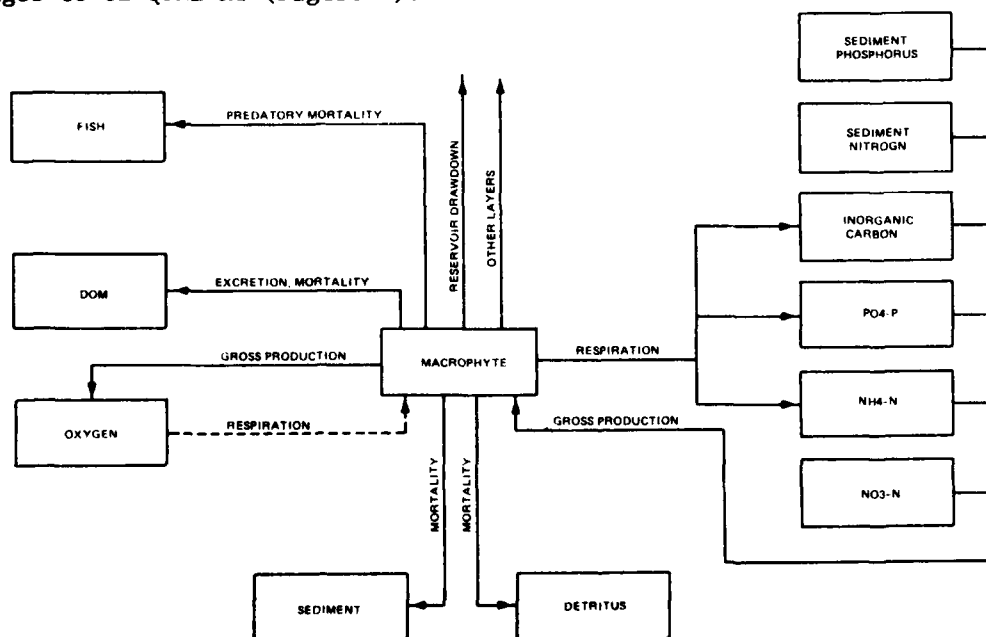


Figure 1. Compartment diagram of macrophyte model recommended for CE-QUAL-R1

## Report composition

6. In the following section the specific physiological processes recommended for inclusion in a new macrophyte subroutine are formulated for incorporation into CE-QUAL-R1. Next, a geometric scheme for apportioning macrophyte biomass among model layers is discussed. The next major section contains recommendations for the simulation of macrophyte control measures (mechanical harvesting, herbicidal treatment). The next section discusses the validation of select process formulations based upon published data on two macrophyte species, *Myriophyllum spicatum* and *Hydrilla verticillata*. The final section summarizes the major recommendations contained in this report. Two appendices are also included. Appendix A presents equations included in a stand-alone version of the macrophyte submodel used in the process validation studies, while Appendix B lists representative values for parameters included in the proposed macrophyte submodel based on published research on *M. spicatum* and *H. verticillata*. The material contained in this report will be included in a final, revised edition of the CE-QUAL-R1 User's Manual (Environmental Laboratory 1982) scheduled for publication in 1985.

## Recommended Physiologic Processes

7. The differential equation for the macrophyte state variable expresses conservation of mass in each horizontal model layer. The solution provides material concentrations as functions of time and depth. The equation is mathematically expressed as follows:

$$\left[ \begin{array}{l} \text{rate of} \\ \text{change} \\ \text{of mass} \\ \text{g day}^{-1} \end{array} \right] = \left[ \begin{array}{l} \text{macrophyte} \\ \text{biomass} \end{array} * \begin{array}{l} \text{gross} \\ \text{production} \\ \text{rate} \end{array} - \begin{array}{l} \text{dark} \\ \text{respiration} \\ \text{rate} \end{array} - \begin{array}{l} \text{photorespiration} \\ \text{rate} \end{array} \right. \\ \left. - \begin{array}{l} \text{grazing} \\ \text{rate} \end{array} - \begin{array}{l} \text{nonpredatory} \\ \text{mortality} \\ \text{rate} \end{array} - \begin{array}{l} \text{mechanical} \\ \text{or} \\ \text{chemical} \\ \text{harvesting} \\ \text{rate} \end{array} \right] \quad (1)$$

Each of the individual terms in this equation is discussed in the subsections which follow. The style of presentation follows that contained in the

CE-QUAL-R1 User's Manual (Environmental Laboratory 1982) which should be consulted for further details. The overall structure of CE-QUAL-R1 will not be presented here. Only those macrophyte process terms specifically included in the proposed new macrophyte submodel will be documented plus their interactions with other compartments in CE-QUAL-R1.

#### Macrophyte processes

8. Gross production. The daily photosynthetic or gross production rate is a function of temperature, light intensity, and nutrient concentration:

$$PLTGRO = PLTMAX * RMULT1(T) * RMULT2(T) * MIN(XLIMN, XLIMP, XLIMC) * XLIML \quad (2)$$

where

PLTGRO = photosynthetic rate, day<sup>-1</sup>

PLTMAX = user-specified maximum photosynthetic rate, day<sup>-1</sup>

RMULT1,2(T) = temperature limitation functions, unitless

XLIMN = limitation function for nitrogen, unitless

XLIMP = limitation function for phosphorus, unitless

XLIMC = limitation function for carbon, unitless

XLIML = limitation function for light intensity, unitless

9. Temperature limitation is calculated using the equations developed by Thornton and Lessem (1978):

$$\begin{aligned}
 RMULT1(T) &= \begin{cases} 0 & T \leq T_1 \\ \frac{K_1 e^{\lambda_1 (T - T_1)}}{1 + K_1 e^{\lambda_1 (T - T_1)} - 1} & T > T_1 \end{cases} \\
 RMULT2(T) &= \begin{cases} \frac{K_4 e^{\lambda_2 (T_4 - T)}}{1 + K_4 e^{\lambda_2 (T_4 - T)} - 1} & T < T_4 \\ 0 & T \geq T_4 \end{cases}
 \end{aligned} \quad (3)$$

where

$$\lambda_1 = \frac{1}{T_2 - T_1} \ln \frac{K_2(1 - K_1)}{K_1(1 - K_2)}$$

$$\lambda_2 = \frac{1}{T_4 - T_3} \ln \frac{K_3(1 - K_4)}{K_4(1 - K_3)}$$

As is the case in the parent model CE-QUAL-R1,  $T_1$  and  $T_4$  represent the user-specified lower and upper lethal temperatures for the processes in question, while  $T_2$  and  $T_3$  (also user specified) define the range of optimum temperatures over which the process occurs at near the maximum rate (Environmental Laboratory 1982). The term  $T$  represents the computed temperature of a specific layer in the model CE-QUAL-R1. The corresponding user-specified  $K$  values define the relative rates (i.e., on a 0 to 1 basis) at which the process occurs at each of these temperatures.

10. Nutrient limitation is dependent upon the concentrations of nitrogen and phosphorus in the water column and sediment and on the carbon concentration in the water column. The nutrient determined to be limiting based upon the following Monod equation is used in the photosynthesis calculation (Equation 2):

$$XLIM(N,C,P) = \frac{C}{K_{1/2} + C} \quad (4)$$

where

$XLIM(N,C,P)$  = nutrient limitation function for nitrogen, carbon, and phosphorus, unitless

$C$  = concentration of respective nutrient in the water column ( $N$ ,  $C$ ,  $P$ ) or sediment ( $N$ ,  $P$ ),  $g\ m^{-3}$

$K_{1/2}$  = user-specified half-saturation coefficient for the respective nutrient,  $g\ m^{-3}$

The limiting nutrient is defined in this context as the one giving the minimum value of Equation 4.

11. Many nutrients used by freshwater submersed macrophytes, including both nitrogen and phosphorus, are obtained primarily through the roots from sediment (Best and Mantai 1978; Bole and Allan 1978; Carignan and Kalff 1980; DeMarte and Hartman 1974; Nichols and Kinney 1976). CE-QUAL-R1 has

## APPENDIX A: MACROPHYTE MODEL STAND-ALONE VERSION

### Introduction

1. A stand-alone version of the macrophyte model was developed to verify and validate several of the recommended process equations for a single model layer. This appendix provides a list of the state variable equations used in this version of the model. Seven compartments are represented by the model, including macrophytes, dissolved oxygen, particulate organic matter (POM), dissolved organic matter (DOM), phosphorus, nitrogen, and organic sediment. The individual process equations which together comprise the state variable equations are also described herein. A parameter list (Table A1) describes each of the parameters used in the process equations and the values used in running the stand-alone version.

2. The macrophyte process equations correspond to those given in the main body of this report (although several variable names have been changed in this version of the model). Equations for the other six state variables contain terms reflecting the impacts of macrophyte processes on other components of aquatic ecosystems. This stand-alone version of the model is appropriate for implementation on a microcomputer.

3. There are some differences between the stand-alone version of the model and that recommended for CE-QUAL-R1. For the stand-alone version, (a) it was assumed that macrophyte production was not nutrient limited, (b) contributions to nutrients from macrophyte respiration were not included, and (c) contributions to nutrients from macrophyte nonpredatory mortality are included. Additionally, CE-QUAL-R1 does not include harvesting as the stand-alone version does.

- Ikusima, I. 1965. "Ecological Studies on the Productivity of Aquatic Plant Communities. I. Measurement of Photosynthetic Activity," Botanical Magazine of Tokyo, Vol 78, pp 202-211.
- Jewell, W. J. 1971. "Aquatic Weed Decay: Dissolved Oxygen Utilization and Nitrogen and Phosphorus Regeneration," Journal of Water Pollution Control Federation, Vol 43, pp 1457-1467.
- McGahee, C. F., and Davis, G. J. 1971. "Photosynthesis and Respiration in *Myriophyllum spicatum* L. as Related to Salinity," Limnology and Oceanography, Vol 16, pp 826-829.
- Miller, A. 1981. "Prediction of *Hydrilla* Growth and Biomass for Mechanical Harvesting Operations," Proceedings, 15th Annual Meeting, Aquatic Plant Control Research Planning and Operations Review, Miscellaneous Paper A-81-3, US Army Engineer Waterways Experiment Station, Vicksburg, Miss.
- Nichols, D. S., and Keeney, D. R. 1976. "Nitrogen Nutrition of *Myriophyllum spicatum*: Variation of Plant Tissue Nitrogen Concentration with Season and Site in Lake Wingra," Freshwater Biology, Vol 6, pp 137-144.
- Olah, J. 1972. "Leaching, Colonization and Stabilization During Detritus Formation," Mem. Ist. Ital. Idrobiol., Vol 29, pp 105-127.
- Otsuki, A., and Hanya, T. 1972. "Production of Dissolved Organic Matter from Dead Green Algal Cells. I. Aerobic Microbial Decomposition," Limnology and Oceanography, Vol 17, pp 248-257.
- Stanley, R. A., and Naylor, A. W. 1972. "Photosynthesis in Eurasian Water-milfoil (*Myriophyllum spicatum* L.)," Plant Physiology, Vol 50, pp 149-151.
- Steele, J. H. 1962. "Environmental Control of Photosynthesis in the Sea," Limnology and Oceanography, Vol 7, pp 137-150.
- Strickland, J. D. H. 1960. "Measuring the Production of Marine Phytoplankton," Bulletin of the Fishery Research Board of Canada, Vol 122, 172 pp.
- Thornton, K. W., and Lessem, A. S. 1978. "A Temperature Algorithm for Modifying Biological Rates," Transactions of the American Fishery Society, Vol 107, pp 284-287.
- Van, T. K., Haller, W. T., and Bowes, G. 1976. "Comparison of the Photosynthetic Characteristics of Three Submersed Aquatic Plants," Plant Physiology, Vol 58, pp 761-768.
- Wetzel, R. G., and Manny, B. A. 1975. "Secretion of Dissolved Organic Carbon and Nitrogen by Aquatic Macrophytes," Verh. Internat. Verein. Limnol., Vol 18, pp 162-170.
- Wile, I. 1978. "Environmental Effects of Mechanical Harvesting," Journal of Aquatic Plant Management, Vol 16, pp 14-20.



Brylinsky, M., and Mann, K. H. 1973. "An Analysis of Factors Governing Productivity in Lakes and Reservoirs," Limnology and Oceanography, Vol 18, pp 1-14.

Carignan, R., and Kalff, J. 1980. "Phosphorus Sources for Aquatic Weeds: Water or Sediments?" Science, Vol 207, pp 987-989.

Carpenter, S. R. 1976. Some Environmental Impacts of Mechanical Harvesting of Nuisance Submersed Vascular Plants, Unpublished M.S. Thesis, University of Wisconsin.

Carpenter, S. R. 1980. "Enrichment of Lake Wingra, Wisconsin, by Submersed Macrophyte Decay," Ecology, Vol 6, pp 1145-1155.

de la Cruz, A. A., and Gabriel, B. C. 1974. "Caloric, Elemental, and Nutritive Changes in Decomposing *Juncus roemerianus* Leaves," Ecology, Vol 55, pp 882-886.

DeMarte, J. A., and Hartman, R. T. 1974. "Studies on Absorption of P, Fe, and Ca by Water Milfoil (*Myriophyllum exalbescent*, Fernald)," Ecology, Vol 55, pp 188-194.

Environmental Laboratory. 1982. "CE-QUAL-R1: A Numerical One-Dimensional Model of Reservoir Water Quality; A User's Manual," Instruction Report E-82-1 (Revised Edition; Supersedes Instruction Report E-82-1 dated April 1982), US Army Engineer Waterways Experiment Station, Vicksburg, Miss.

Fitzgerald, G. P. 1964. "The Effect of Algae on BOD Measurements," National Pollution Control Federation Journal, Vol 36, pp 1524-1542.

Godshalk, G. L., and Wetzel, R. G. 1978. "Decomposition of Aquatic Angiosperms. I. Dissolved Components," Aquatic Botany, Vol 5, pp 281-300.

Hanlon, R. D. G. 1972. "The Breakdown and Decomposition of Allochthonous and Autochthonous Plant Litter in an Oligotrophic Lake," Hydrobiologia, Vol 88, pp 218-288.

Hargrave, B. T. 1972. "Aerobic Decomposition of Sediment and Detritus as a Function of Particle Surface Area and Organic Content," Limnology and Oceanography, Vol 17, pp 583-596.

Harrison, P. G., and Mann, K. H. 1975. "Detritus Formation From Eelgrass (*Zostera marina* L.): The Relative Effects of Fragmentation, Leaching and Decay," Limnology and Oceanography, Vol 20, pp 924-935.

Healey, F. P. 1976. "Ammonium and Urea Uptake by Some Freshwater Algae," Canadian Journal of Botany, Vol 55, pp 61-69.

Healey, F. P., and Hendzel, L. L. 1975. "Effect of Phosphorus Deficiency on Two Algae Growing in Chemostats," Journal of Phycology, Vol 11, pp 303-309.

### Recommendations

31. It is recommended that the model for submersed aquatic plants described in this report be incorporated in the CE-QUAL-R1 model with due consideration of the following points:

- a. The light response function should permit representation of photoinhibition (this same algorithm should be used for algae in CE-QUAL-R1).
- b. Because nutrients are an explicit part of the photosynthesis algorithm, limitation should be based on the Monod function for the nutrient shown to be limiting using threshold ratios.
- c. The spatial relationships of the rooted zone of macrophytes to the model layers should be accounted for based on the intersection of model layers with the reservoir bottom, creating a two-dimensional array of cells for macrophyte computations; the macrophytes should be apportioned into the vertical layers based on cell-by-cell computations and a comparison with a user-specified maximum macrophyte density in each cell; this algorithm can also be used to determine the biomass of macrophytes cut by a mechanical harvester set at a particular depth.
- d. Chemical control can be modeled using dose-response relationships.

### References

- Adams, M. S., Titus, J., and McCracken, M. 1974. "Depth Distribution of Photosynthetic Activity in a *Myriophyllum spicatum* Community in Lake Wingra," Limnology and Oceanography, Vol 19, No. 3, pp 377-389.
- Barko, J. W., and Smart, R. M. 1980. "Mobilization of Sediment Phosphorus by Submersed Freshwater Macrophytes," Freshwater Biology, Vol 10, pp 229-238.
- Barko, J. W., Smart, R. M., Hardin, D. G., and Matthews, M. S. 1980. "Growth and Metabolism of Three Introduced Submersed Plant Species in Relation to the Influences of Temperature and Light," Technical Report A-80-1, US Army Engineer Waterways Experiment Station, Vicksburg, Miss.
- Best, M. D., and Mantai, K. E. 1978. "Growth of *Myriophyllum*: Sediment or Lake Water as the Source of Nitrogen and Phosphorus?" Ecology, Vol 59, pp 75-80.
- Bole, J. B., and Allan, J. R. 1978. "Uptake of Phosphorus from Sediment by Plants, *Myriophyllum spicatum* and *Hydrilla verticillata*," Water Research, Vol 12, pp 353-358.
- Bowes, G., Van, T. K., Ganard, L. A., and Haller, W. T. 1977. "Adaptation to Low Light Levels by *Hydrilla*," Journal of Aquatic Plant Management, Vol 15, pp 32-35.

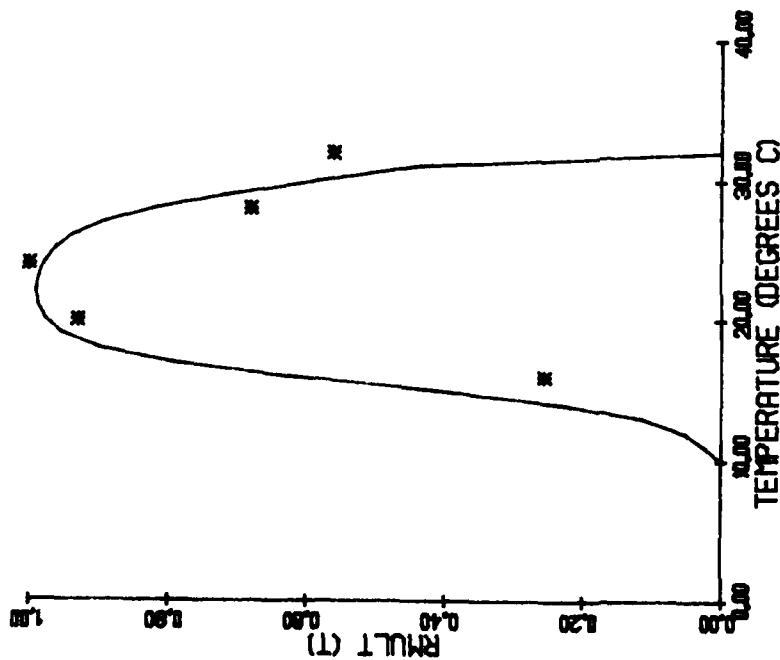


Figure 5. Process validation plot using the Thornton and Lessem (1978) equation, RMULT, as a temperature rate multiplier to predict the effect of temperature on photosynthetic rate. Asterisks represent normalized experimental results from Barko et al. (1980). Process parameter values are given in text

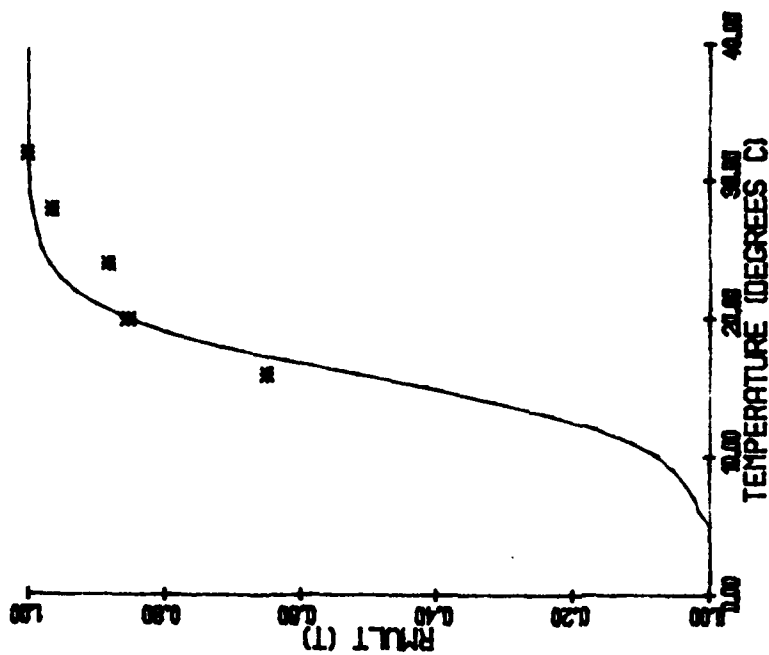


Figure 6. Process validation plot using the rising limb of the Thornton and Lessem (1978) equation, RMULT, as a temperature rate multiplier to predict the effect of temperature on dark respiration rate. Asterisks represent the normalized experimental results from Barko et al. (1980) for *H. verticillata*. Process parameter values are given in text

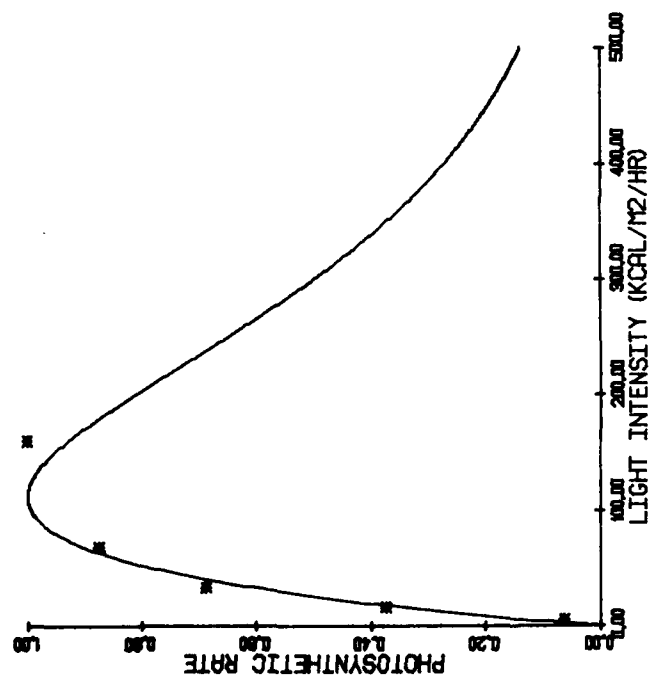


Figure 3. Process validation plot using Steele's (1962) equation to represent the photosynthetic light intensity response of *M. spicatum*. Asterisks represent normalized experimental results from Van, Haller, and Bowes (1976). Process parameter values are given in text

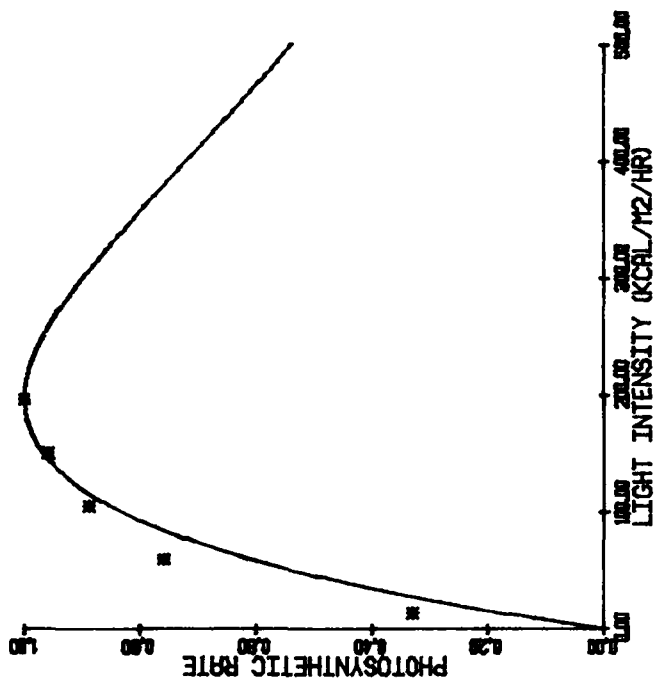


Figure 4. Process validation plot using Steele's (1962) equation to represent the photosynthetic light intensity response of *H. verticillata*. Asterisks represent normalized experimental results from Barko et al. (1980). Process parameter values are given in text

Depending on how the chemical control program is implemented, the macrophyte mass killed can be transferred as appropriate to other model compartments (detritus, sediment, dissolved organic matter).

#### Process Validation

27. Select process equations included in the proposed macrophyte sub-model have been validated based on experimental results from the literature and published experimental results performed at the US Army Engineer Waterways Experiment Station by Dr. John Barko and colleagues. Data on two macrophyte species of particular interest to the Corps were used in this validation procedure, *M. spicatum* and *H. verticillata*. Results of validating several specific equations in the macrophyte model are discussed in the following paragraphs.

28. The equation used to represent the photosynthetic light response is that of Steele (1962) (see Equation 5 and Appendix B). Figures 3 and 4 demonstrate that this equation fits experimental data from Van, Haller, and Bowes (1976) for *M. spicatum* and from Barko et al. (1980) for *H. verticillata*. The parameter PISAT, which describes the saturating light intensity for photosynthesis, was set at 112 and 196 kcal m<sup>-2</sup> hr<sup>-1</sup>, respectively, for *M. spicatum* and *H. verticillata* (Appendix B). Photoinhibition at high light intensities can also be predicted using this equation. Although this type of response of these two species to high light intensities has not been observed, other species demonstrate photoinhibition which could be significant during reservoir drawdown.

29. The effect of temperature on photosynthesis is represented using the equation of Thornton and Lessem (1978) (Equation 3). Validation of this equation for *H. verticillata*, based on results of Barko et al. (1980), is demonstrated in Figure 5. The parameter values used in this equation are as follows: T1 = 10°C, T2 = 20°C, T3 = 24°C, T4 = 32°C, K1 = 0.01, K2 = 0.98, K3 = 0.98, and K4 = 0.30 (Appendices A and B).

30. Validation of the equation representing dark respiration (Equation 6) is represented in Figure 6 for *H. verticillata*. The parameter values used are as follows: T1 = 5°C, T2 = 25°C, K1 = 0.01, and K2 = 0.98 (Appendix B).

The index J ranges from 1 (top layer) up to a user-specified value indicating the maximum number of layers in which macrophytes can occur (actually, the maximum rooting depth in metres). If all the mass in that column can be contained in the bottommost cell, it is placed there. Otherwise, Equation 9 is iterated (i.e., the value of J is increased sequentially) until the calculated total macrophyte mass for that column is apportioned among cells in that column, such that the mass in each cell is less than or equal to the maximum calculated with Equation 9. The total macrophyte mass is then calculated for each model layer by summation, and for the entire reservoir.

#### Management Control Processes

25. In addition to ecological processes, the model can also simulate management control processes including mechanical harvesting and chemical control of the plants. Macrophyte mass removed by mechanical harvesting is a function of plant rooting depth and mass density as well as the cutting depth of the mechanical harvester. Having determined macrophyte biomass in each model layer, the amount cut (MBIOCUT) by a mechanical harvester set at a particular cutting depth (CUTZ) can be calculated by summation. If the cutting depth falls between layer boundaries, then an appropriate fraction of the macrophyte mass in that layer can be removed since mass is assumed to be distributed homogeneously within layers.

26. Chemical control is a function of the following dose-response curve for the herbicide used:

$$MCHEM(I) = MACRO(I) * CHEM / (LC50 + CHEM) \quad (10)$$

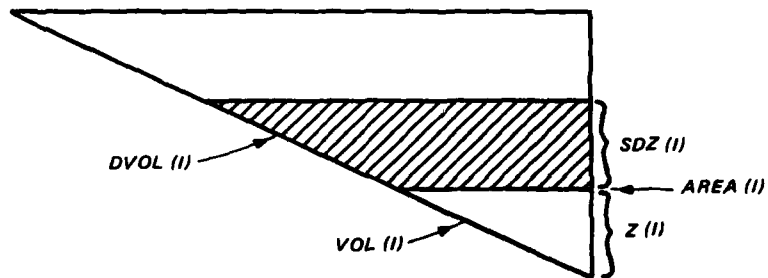
where

MCHEM(I) = macrophyte biomass killed in layer I, g

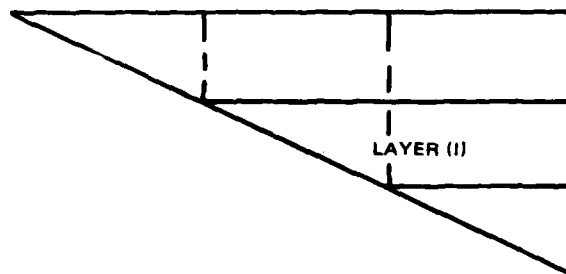
MACRO(I) = total macrophyte biomass in layer I, g

CHEM = user-specified ambient environmental concentration of herbicide applied,  $\mu\text{g l}^{-1}$

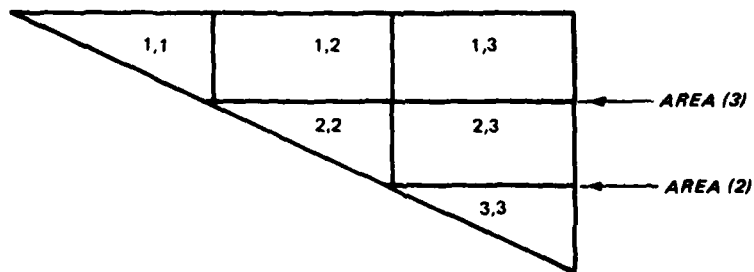
LC50 = user-specified herbicide concentration which will kill 50 percent of the macrophytes,  $\mu\text{g l}^{-1}$



a. VARIABLE LAYERS



b. VERTICAL SEGMENTS



c. CELL VOLUMES

Figure 2. Model structure for macrophyte distribution

the Ith layer. The actual volume of the Ith layer, DVOL(I), is calculated as the difference between VOL(I+1) and VOL(I). Both volume and area are typically represented as power functions of elevation.

23. Using this scheme, a series of vertical segments or columns can be superimposed at the points at which boundary layers intersect the reservoir bottom (Figure 2b), creating a series of two-dimensional cells for macrophyte computations (Figure 2c). To simplify the computational sequence, these cells are numbered from the reservoir surface down, and from upstream toward the dam. A given cell is indexed (i,j) with i referring to row position and j to column. Because each of the layers in the model representation of a reservoir is extremely long and thin, the bottom surface area in which macrophytes root can be approximated as the difference AREA(I+1) - AREA(I). Similarly, the volume of each computational cell can be approximated as this bottom surface area times the thickness (SDZ) of the layer in which that cell occurs. These bottom areas and cell volumes are used in macrophyte computations as described in the following paragraph.

24. Macrophytes are associated with the bottom sediments in which they are rooted and with the overlying water column. In order to determine how macrophyte mass is apportioned among the cells in a given vertical column, the assumption is made that the volumetric density of macrophyte dry mass cannot exceed a user-specified maximum value (PLDENS,  $\text{g m}^{-3}$ ). At each model time step, the macrophyte differential equation (Equation 1) is solved on a cell-by-cell basis using a simple Euler procedure and the mass is calculated at the previous time step as an initial value. Then macrophyte mass is summed over all cells in a given column. Beginning with the bottommost cell (i.e., the one nearest the sediment), this summed mass is apportioned among cells by comparing it with the maximum mass which each cell can contain. For cells in the Ith column, this maximum is calculated as

$$\text{DATA}(J,I) = \text{PLDENS} * \text{SDZ}(J) * (\text{AREA}(I+1) - \text{AREA}(I)) \quad (9)$$

where

DATA(J,I) = maximum macrophyte mass which can be contained in the cell in layer J and column I, g

PLDENS = user-specified maximum macrophyte volumetric density,  $\text{g m}^{-3}$

SDZ(J) = thickness of Jth model layer, m

AREA(I) = bottom surface area at layer I,  $\text{m}^2$



coefficients are involved. In a similar manner, grazing represents a direct transfer of mass to fish, without conversion. As a consequence of nonpredatory mortality, macrophyte biomass is transferred to dissolved organic matter, detritus, and sediment compartments. The "dead" biomass is apportioned between the three receiver compartments based on user-specified coefficients.

20. Included in Appendix A is a stand-alone version of the macrophyte model which was used in validating the various process equations just discussed. In addition to containing the equations describing macrophyte physiological processes (Equations 1-8), this version of the model also contains equations for oxygen, particulate organic matter, dissolved organic matter, phosphorus, nitrogen, and sediment. This model thus illustrates the way in which macrophyte terms enter into equations for other water quality constituents included in CE-QUAL-R1. In Appendix B, representative values for the parameters included in Equations 1-8 of the macrophyte model (as defined in Appendix A) are listed, based on research on two macrophyte species of particular interest, *Myriophyllum spicatum* and *Hydrilla verticillata*. CE-QUAL-R1-related parameters and coefficient values are also listed in Appendix B.

#### Spatial Relationships

21. In order to describe vertical growth of macrophytes in a one-dimensional, variable-layer model like CE-QUAL-R1, it was necessary to devise a means of geometrically segmenting the model into a matrix of rows (layers) and columns. This matrix defines the volume of each segment and the proximity of one segment to another. A description of how the matrix can be incorporated into the CE-QUAL-R1 model follows.

22. CE-QUAL-R1 is a one-dimensional model with multiple layers. Thermal energy and materials are assumed to be uniformly distributed within each model layer. Reservoir morphometry is represented in the model by a variable-layer approach (i.e., layer dimensions vary over time based on inflows and outflows and on user-specified morphometric relationships of area and volume to elevation above the reservoir bottom). Relationships among elevation, area, and volume are depicted in Figure 2a. A given layer (numbered I, from the bottom up) is specified as being Z(I) metres above the bottom and SDZ(I) metres thick. The area of the Ith layer, AREA(I), is defined at the lower boundary of that layer. A volume, VOL(I), is also defined up to the lower surface of

7

calculated as the product of the two temperature limitation functions, RMULT1 and RMULT2 (Equation 3), times a user-specified maximum fish grazing rate, times a Monod function similar in form to Equation 4. In this fish-grazing limitation function, the role of  $C$  (Equation 4) is played by the sum, over all types of food (including macrophytes) ingested by fish, of products of a user-specified preference factor for that food type and the concentration of that food type. For this grazing function,  $K_{1/2}$  (in Equation 4) would again be a user-specified half-saturation coefficient for fish grazing. The reader should consult the CE-QUAL-R1 User's Manual (Environmental Laboratory 1982) for further details. An additional preference factor would need to be included in the model, specifying the fractional preference of fish for macrophytes.

#### Interactions with other compartments in CE-QUAL-R1

18. As depicted in Figure 1, those macrophyte processes discussed above also impact a variety of other compartments in CE-QUAL-R1. Thus, corresponding to the process equations given above (Equations 1-8), terms will need to be added to or subtracted from other equations in the model. These terms represent the addition or removal of mass to or from other compartments in the modeled reservoir. These terms will be briefly described here. Although the actual equations will not be provided, they correspond exactly to the form of the equations listed previously.

19. As a result of macrophyte photosynthetic processes, oxygen is evolved. This is modeled as an "equivalent oxygen concentration," calculated as the product at the gross production rate of concentration and a user-specified oxygen-to-biomass stoichiometric coefficient, which is added directly to the oxygen differential equation. Similarly, dark respiration removes oxygen. This removal, a subtraction from the oxygen equation, is calculated as the product of the dark respiration rate of concentration and another user-specified stoichiometric coefficient. Gross production and respiration also result in the uptake and release, respectively, of nutrients (N, P, C) from and to the water column and sediments (Figure 1). These transfers are calculated as the product of the production and respiration rates of concentration and user-specified nutrient-to-biomass stoichiometric coefficients. Photorespiration represents a direct addition of mass to the ammonia-nitrogen, phosphorus, and dissolved organic matter compartments; no conversion

mathematically using only the rising limb of the temperature equation of Thornton and Lessem (1978) (Equation 3):

$$MRESP = MKRESP * RMULT1(T) \quad (6)$$

where

MRESP = dark respiration rate, day<sup>-1</sup>

MKRESP = user-specified maximum dark respiration rate, day<sup>-1</sup>

15. Photorespiration. Photorespiration or excretion is important because it results in the phenomenon known as "nutrient pumping," whereby nutrients are transferred from bottom sediments to water. This process also increases the amount of organic matter dissolved in the water column. Excretion is a function of light intensity. Under conditions of very high or very low light intensities, the rate of extracellular release increases. Mathematically this is represented as

$$MEXCR = (1 - XLIML) * MKEXCR \quad (7)$$

where

MEXCR = excretion rate, day<sup>-1</sup>

MKEXCR = user-specified maximum excretion rate, day<sup>-1</sup>

16. Nonpredatory mortality. Nonpredatory mortality is temperature-dependent when the change in temperature (increase or decrease) over a 7-day period exceeds a critical maximum temperature TMPMAX. Therefore, if  $|TMPTUR(1) - TMPTUR(7)| > TMPMAX$ :

$$MMORT = MKMORT \quad (8)$$

where

TMPTUR(1) and TMPTUR(7) = water temperature over 7-day period, °C

TMPMAX = maximum temperature change, °C

MMORT = nonpredatory mortality rate, day<sup>-1</sup>

MKMORT = user-specified maximum nonpredatory mortality rate, day<sup>-1</sup>

17. Grazing. Grazing of macrophytes by fish is modeled with the same type of grazing function as used in CE-QUAL-R1. Thus, the grazing rate is

compartments representing sediment nitrogen and phosphorus; therefore, limitation of nutrients obtained through the roots can occur, although this is rare in nature. This process is most important in allowing "nutrient pumping" from the sediments into the water column.

12. In some cases where nutrient concentrations in the water are high, it becomes advantageous for the plant to draw nutrients from the water column. In water with a phosphorus concentration of  $2.0 \text{ mg l}^{-1}$ , characteristic of eutrophic reservoirs, *Myriophyllum spicatum* took phosphorus from the water column (Bole and Allan 1978). This is modeled using a species-specific parameter to indicate the water concentration above which nutrients are taken from the water column. Whenever the water column concentration of nitrogen or phosphorus equals or exceeds this user-specified concentration, it is the water concentration of that nutrient which is entered into the Monod equation (Equation 4). Otherwise, it is the sediment concentration of nitrogen or phosphorus which is used in Equation 4.

13. Light limitation is represented using Steele's equation (1962):

$$XLIML = \left( \frac{0.5 * SWSA}{PISAT} \right) \exp \left[ 1 - \left( \frac{0.5 * SWSA}{PISAT} \right) \right] \quad (5)$$

where

SWSA = average irradiance for a specific model layer,  $\text{kcal m}^{-2} \text{ hr}^{-1}$   
(calculated in Subroutine HEAT in CE-QUAL-R1)

PISAT = user-specified irradiance level at which the photosynthetic rate is saturated (i.e., occurs at maximum rate),  $\text{kcal m}^{-2} \text{ hr}^{-1}$

The coefficient value 0.5 is used in Steele's equation to represent the fraction of total irradiance that is photosynthetically active radiation (PAR). PAR is in the range of 400 to 700 nm. Steele's equation can predict photoinhibition of photosynthesis at high light intensities, above the level specified by PISAT. Solar radiation is distributed vertically in the water column in CE-QUAL-R1 based upon the extinction coefficient for water. Light is also attenuated by self-shading by algae, zooplankton, detritus, and suspended solids. An additional self-shading coefficient should be included in the model to account for the effect of macrophyte biomass on light attenuation.

14. Dark respiration. Dark respiration is a function of temperature. As with other respiratory rates in CE-QUAL-R1, it is represented

## State Variable Equations\*

### Macrophyte

$$\dot{\text{MACRO}} = \text{MPROD} - \text{MRESP} - \text{MEXCR} - \text{MMORT} - \text{MHVST}$$

macrophyte = photosynthesis - dark respiration - excretion (photo-respiration) - mortality - harvesting

### Oxygen

$$\dot{\text{OXYGEN}} = \text{OTST} + \text{OMAC} - \text{ANIT} - \text{OPDK} - \text{ODDK} - \text{OSDK}$$

Oxygen = oxygen saturation + contribution from macrophytes

- equivalent loss from nitrogen decay - equivalent loss from POM decay

- equivalent loss from DOM decay - equivalent loss from sediment decay

### Particulate organic matter

$$\dot{\text{POM}} = \text{PMAC} - \text{PDK} - \text{PSTL}$$

POM = contribution from macrophyte mortality and harvesting

- loss from POM decay - loss from settling

### Dissolved organic matter

$$\dot{\text{DOM}} = \text{DMAC} + \text{DEXCR} + \text{DDK} - \text{DBAC}$$

DOM = contribution from macrophyte mortality and harvesting + contribution from macrophyte excretion + contribution from POM decay - loss from bacterial respiration

### Phosphorus (water column)

$$\dot{\text{PO4}} = \text{FMAC} + \text{FDK} + \text{FEXCR} - \text{FSINK}$$

PO4 = contribution from macrophyte mortality and harvesting + contribution from decay of POM and sediments + contribution from macrophyte excretion - loss to algal production

---

\* Each equation represents the time rate of change of the state variable for a model layer. The units of MACRO are grams per square metre per day per model layer. The units of all other state variables are grams per square metre per day per metre of model layer.

### Nitrogen (water column)

$$\dot{N} = NMAC + NDK + NEXCR - NSINK$$

N = contribution from macrophyte mortality and harvesting  
+ contribution from decay of POM and sediments  
+ contribution from macrophyte excretion - loss to algal production

### Organic sediment

$$\dot{SED} = SMAC - SDK$$

SED = contribution from macrophyte mortality and harvesting  
- loss from sediment decay

### Process Equations

#### Macrophyte

$$MPROD = PMAX * RMULT1(T) * RMULT2(T) * LIGHT * MACRO$$

where

PMAX = maximum photosynthetic rate, day<sup>-1</sup>

RMULT1(T) = temperature limitation function, unitless

RMULT2(T) = temperature limitation function, unitless

T = ambient water temperature, °C

LIGHT = light limitation function, unitless

MACRO = macrophyte biomass, g m<sup>-2</sup>

$$LIGHT = \frac{e}{\epsilon(Z2-Z1)} \left\{ e^{\left[ \frac{(-0.5 \cdot IO)}{ISAT} e^{-\epsilon Z2} \right]} - e^{\left[ \frac{(-0.5 \cdot IO)}{ISAT} e^{-\epsilon Z1} \right]} \right\}$$

where

$\epsilon$  = extinction coefficient

Z2 = depth at the bottom of the simulated section, m

Z1 = depth at the top of the simulated section, m

IO = irradiance at the water surface, kcal m<sup>-2</sup> sec<sup>-1</sup>

ISAT = saturating irradiance for photosynthesis, kcal m<sup>-2</sup> sec<sup>-1</sup>

$$MRESP = KRESP * RMULT1(T) * MACRO$$

where

KRESP = user-specified maximum respiration rate,  $g\ g^{-1}\ day^{-1}$

$$MEXCR = KEXCR * (1-LIGHT) * MACRO$$

where

KEXCR = user-specified maximum excretion rate,  $g\ g^{-1}\ day^{-1}$

If,  $|TMPTUR(1) - TMPTUR(7)|$  is greater than TMPMAX, then

$$MMORT = KMORT * MACRO$$

where

KMORT = nonpredatory mortality rate,  $g\ g^{-1}\ day^{-1}$

TMPMAX = critical maximum temperature difference over a 7-day period, °C

TMPTUR(1) and TMPTUR(7) = water temperatures over a 7-day period, °C

$$MHVST = CHEM * MACRO$$

where

CHEM = rate of die-off of macrophyte dependent upon type of chemical used,  $g\ g^{-1}\ day^{-1}$

NOTE: Mechanical harvesting is calculated outside the differential equation as follows:

$$MWH + MACRO = MHT$$

$$Z - MHT = TPLT$$

$$CUTZ - TPLT = MCUT$$

$$MWH + MCUT = MBIOCUT$$

where

MWH = species-specific weight-to-height ratio,  $\text{g m}^{-1}$   
MHT = macrophyte height, m  
Z = depth of water column, m  
TPLT = top of plant, m  
CUTZ = cutting depth of mechanical harvester, m  
MCUT = amount of macrophyte cut, m  
MBIOCUT = biomass of macrophyte cut,  $\text{g m}^{-2}$

#### Oxygen

OTST =  $(14.6 * \exp(-(0.027767 - 0.00027 * T + 0.000002 * T * T) * T)) * Z$   
OMAC =  $(\text{OMACEQ1} * \text{MPROD}) - (\text{OMACEQ2} * \text{MRESP})$   
ANIT =  $\text{ONEQ} * \text{NMAC}$   
OPDK =  $\text{OPEQ} * \text{PDK}$   
ODDK =  $\text{ODEQ} * \text{DDK}$   
OSDK =  $\text{OSEQ} * \text{SDK}$

#### Particulate organic matter

PMAC =  $(\text{MMORT} * \text{M1}) + (\text{MHVST} * \text{H1})$   
PDK =  $\text{KPOM} * \text{POM} * \text{RMULT1}(T)$   
PSTL =  $(\text{PMSTL} * \text{MMORT}) + (\text{PHSTL} * \text{MHVST})$   
KPOM =  $0.01192 * 1/\text{NTC}(2) + 0.00672$

#### Dissolved organic matter

DMAC =  $(\text{MMORT} * \text{M2}) + (\text{MHVST} * \text{H2})$   
DEXCR =  $\text{MEXCR} * \text{E2}$   
DDK =  $\text{PDK} * \text{P2}$   
DBAC =  $\text{KDOM} * \text{DOM} * \text{RMULT1}(T)$   
KDOM =  $0.024 * 1/\text{NTC}(3) + 0.0192$

#### Phosphorus

FMAC =  $(\text{MMORT} * \text{M3}) + (\text{MHVST} * \text{H3})$   
FDK =  $(\text{PDK} * \text{P3}) + (\text{SDK} * \text{S3})$   
FEXCR =  $\text{MEXCR} * \text{E3}$   
FSINK =  $\text{photoplankton biomass} * \text{FRS}$



Nitrogen

$$\text{NMAC} = (\text{MMORT} * \text{M4}) + (\text{MHVST} * \text{H4})$$

$$\text{NDK} = (\text{PDK} * \text{P4}) + (\text{SDK} * \text{S4})$$

$$\text{NEXCR} = \text{MEXCR} * \text{E4}$$

$$\text{NSINK} = \text{photoplankton biomass} * \text{NRS}$$

Sediments

$$\text{SMAC} = (\text{MMORT} * \text{M5}) + (\text{MHVST} * \text{H5})$$

$$\text{SDK} = \text{KSED} * \text{SED} * \text{RMULT1(T)}$$

$$\text{KSED} = 0.00519 * 1/\text{NTC}(4) + 0.00346$$

Table A1  
Stand-Alone Version Macrophyte Model Parameter List

Parameter	Parameter Description	Value	Reference
Z	Depth of water column, m	Specified by user	
CHDA	Chemical dependent rate of macrophyte die-off, $g\ g^{-1}\ day^{-1}$	Specified by user	
CUTZ	Cutting depth of mechanical cutter, m	Specified by user	
TEMPAX	Critical maximum temperature difference for nonpredatory mortality, $^{\circ}C$	5	Boylan, unpublished data
ISAT	Saturating light intensity for photosynthesis, $kcal\ m^{-2}\ sec^{-1}$	112 196	Van, Haller, and Boves (1976) Barko et al. (1980)
KEKCR	Excretion rate for macrophyte, $g\ g^{-1}\ day^{-1}$	0.023 0.017	Stanley and Naylor (1972) Boves et al. (1977)
KNORT	Mortality rate for macrophyte, $g\ g^{-1}\ day^{-1}$	0.001	Calibrated
KSED	Decay rate for sediment, $g\ g^{-1}\ day^{-1}$	0.001 - 0.015	Hargrave (1972)
KPOM	Decay rate for POM, $g\ g^{-1}\ day^{-1}$	0.007 - 0.06 dead mixed algae 0.002 - 0.007 Potomogeton	Fitzgerald (1964) Hanlon (1972)
KRESP	Respiration rate for macrophyte, $g\ g^{-1}\ day^{-1}$	0.027 0.016 - 0.039	Boves et al. (1977) McGahee and Davis (1971)
KDOM	Decay rate (bacterial respiration) for DOM, $g\ g^{-1}\ day^{-1}$	0.238	Carpenter (1980)
PMAX	Maximum photosynthetic rate, $g\ g^{-1}\ day^{-1}$	0.48 - 0.6 0.02 - 0.6	Van, Haller, and Boves (1976); Ikusima (1965) Adam, Titus, and McCracken (1974)
OMEQ	Oxygen equivalent for nitrogen decay or mineralization, unitless	3.43	Calculated
OPEQ	Oxygen equivalent for POM mineralization or decay, unitless	1.3	Jewell (1971)
ODEQ	Oxygen equivalent for DOM mineralization or decay, unitless	1.3	Jewell (1971)
OSEQ	Oxygen equivalent for sediment mineralization or decay, unitless	1.3	Jewell (1971)

(Continued)

(Sheet 1 of 4)

Table A1 (Continued)

Parameter	Parameter Description	Value	Reference
OMACEQ	Oxygen equivalent for macrophyte photosynthesis and respiration, unitless	1.0 1.2	Brylinsky and Mann (1973) Strickland (1960)
PMSTL	Mortality fraction of POM that sediments	20 to 50%	Calibrated
PMSTL	Harvested fraction of POM that sediments	10 to 40%	Calibrated
NBS	Nitrogen uptake rate by phytoplankton, $g\ g^{-1}\ day^{-1}$	0.012 to 0.035	Healey (1976)
PBS	Phosphorus uptake rate by phytoplankton, $g\ g^{-1}\ day^{-1}$	0.3 to 0.6	Healey and Hendzel (1975)
M1	Fraction of dying macrophyte that goes to POM, unitless	29%	Godshalk and Wetzel (1978)
M2	Fraction of dying macrophyte that goes to DOM, unitless	1 to 10%	Wetzel and Manny (1975)
M3	Fraction of dying macrophyte that goes to phosphorus, unitless	0.13 to 0.60%	Wile (1978)
M4	Fraction of dying macrophyte that goes to nitrogen, unitless	1.2 to 2.8%	Wile (1978)
M5	Fraction of dying macrophyte that goes to sediment, unitless	18%	Carpenter (1976)
H1	Fraction of harvested macrophyte that goes to POM, unitless	Specified by user; dependent on harvesting method	
H2	Fraction of harvested macrophyte that goes to DOM, unitless		
H3	Fraction of harvested macrophyte that goes to phosphorus, unitless		
H4	Fraction of harvested macrophyte that goes to nitrogen, unitless		
H5	Fraction of harvested macrophyte that goes to sediment, unitless		

(Continued)

(Sheet 2 of 4)

Table A1 (Continued)

Parameter	Parameter Description	Value	Reference
E2	Fraction of excretion that goes to phosphorus, unitless	4 to 6% <i>Egeria densa</i> 7 to 29% <i>Hydrilla verticillata</i> 1 to 4% <i>Myriophyllum spicatum</i>	Barko and Smart (1980)
E3	Fraction of excretion that goes to nitrogen, unitless	11%	Wetzel and Manny (1975)
E4	Fraction of excretion that goes to DOM, unitless	1 to 10%	Wetzel and Manny (1975)
P2	Fraction of decaying POM that goes to DOM, unitless	15 to 46%	Godshalk and Wetzel (1978)
P3	Fraction of decaying POM that goes to phosphorus, unitless	0.12%	de la Cruz and Gabriel (1974)
P4	Fraction of decaying POM that goes to nitrogen, unitless	0.40%	de la Cruz and Gabriel (1974)
S3	Fraction of decaying sediment that goes to phosphorus, unitless	0.10 to 0.15%	Calibrated
S4	Fraction of decaying sediment that goes to nitrogen, unitless	0.40 to 1.0%	Calibrated
MACRO	Initial macrophyte biomass, $g\ m^{-2}$	Specified by user	
OXY	Initial oxygen concentration, $g\ m^{-3}$		
POM	Initial POM concentration, $g\ m^{-3}$		
DOM	Initial DOM concentration, $g\ m^{-3}$		
P	Initial phosphorus concentration, $g\ m^{-3}$		
N	Initial nitrogen concentration, $g\ m^{-3}$		
SED	Initial sediment concentration, $g\ m^{-3}$		
K1	Temperature rate factor for photosynthesis and respiration at $T = T_1$	0.01	Calibrated
K2	Temperature rate factor for photosynthesis and respiration at $T = T_2$	0.98	Calibrated

(Continued)

(Sheet 3 of 4)

Table A1 (Concluded)

Parameter	Parameter Description	Value	Reference
K3	Temperature rate factor for photosynthesis at $T = T_3$	0.98	Calibrated
K4	Temperature rate factor for photosynthesis at $T = T_4$	0.30	Calibrated
T1	Critical low temperature for photosynthesis and respiration, °C	10°C	Barko et al. (1980); Van, Haller and Boves (1976)
T2	Optimum low temperature for photosynthesis and respiration, °C	16°C 20°C	Van, Haller, and Boves (1976) Barko et al. (1980)
T3	Optimum high temperature for photosynthesis, °C	24°C	Barko et al. (1980)
T4	Critical high temperature for photosynthesis, °C	32°	Barko et al. (1980)
MMH	Species-specific weight-to-height ratio, g m <sup>-1</sup>	0.78 2.40	Boylan, unpublished data Miller (1981)
NTC(1)	Nitrogen to carbon ratio for macrophytes	0.03 to 0.08	Godshalk and Wetzel (1978)
NTC(2)	Nitrogen to carbon ratio for POM	0.05	Harrison and Mann (1975)
NTC(3)	Nitrogen to carbon ratio for DOM	0.09 to 0.16	Otsuki and Hanya (1972)
NTC(4)	Nitrogen to carbon ratio for sediments	0.06 to 0.16	Olah (1972)

## APPENDIX B: MACROPHYTE MODEL PARAMETER LIST

Tabulated in Table B1 in this Appendix are values for specific parameters included in the state variable and process equations which comprise the macrophyte model proposed in the main body of this report (as intended for inclusion in CE-QUAL-R1). These values were either derived from published literature sources or established in the process validation studies described earlier. Most values tabulated here apply to one or two macrophyte species of interest, *Myriophyllum spicatum* or *Hydrilla verticillata*.

Table B1

## Macrophyte Model Parameter List Recommended for CE-QUAL-R1

Parameter	Description	Species	Value	Converted Value	Reference
PISAT	Saturating light intensity for photosynthesis	<i>M. spicatum</i>	$600 \mu\text{E m}^{-2} \text{ sec}^{-1}$	$112 \text{ kcal m}^{-2} \text{ hr}^{-1}$	Van, Haller, and Boves (1976)
PISAT		<i>M. spicatum</i>	$1050 \mu\text{E m}^{-2} \text{ sec}^{-1}$	$196 \text{ kcal m}^{-2} \text{ hr}^{-1}$	Barko et al. (1980)
PISAT		<i>H. verticillata</i>	$600 \mu\text{E m}^{-2} \text{ sec}^{-1}$	$112 \text{ kcal m}^{-2} \text{ hr}^{-1}$	Van, Haller, and Boves (1976)
PLTMAX	Maximum photo-synthetic rate	<i>M. spicatum</i>	$3.3 \mu\text{mole CO}_2 \text{ mg chl}^{-1} \text{ hr}^{-1}$	$0.04 \text{ g g}^{-1} \text{ hr}^{-1}$	Van, Haller, and Boves (1976)
PLTMAX		<i>M. spicatum</i>	$0.8 - 4.6 \mu\text{mole CO}_2 \text{ mg chl}^{-1} \text{ hr}^{-1}$	$0.09 - 0.05 \text{ g g}^{-1} \text{ hr}^{-1}$	Adams, Titus, and McCracken (1974)
PLTMAX		<i>H. verticillata</i>	$4.6 \mu\text{mole CO}_2 \text{ mg chl}^{-1} \text{ hr}^{-1}$	$0.05 \text{ g g}^{-1} \text{ hr}^{-1}$	Van, Haller, and Boves (1976)
PLTMAX		<i>H. verticillata</i>	$5 \text{ mg CO}_2 \text{ g}^{-1} \text{ hr}^{-1}$	$0.05 \text{ g g}^{-1} \text{ hr}^{-1}$	Ikusima (1965)
MKRESP	Dark respiration	<i>M. spicatum</i>	$2.5 \mu\text{mole CO}_2 \text{ g}^{-1} \text{ hr}^{-1}$	$0.027 \text{ g g}^{-1} \text{ hr}^{-1}$	Boves et al. (1977)
MKRESP	Dark respiration	<i>H. verticillata</i>	$1.5 - 3.6 \mu\text{moles mg chl}^{-1} \text{ hr}^{-1}$	$0.016 - 0.039 \text{ g g}^{-1} \text{ hr}^{-1}$	McGahee and Davis (1971)
MKEXCR	Photorespiration rate	<i>M. spicatum</i>	$0.023 \text{ g g}^{-1} \text{ hr}^{-1}$	$0.023 \text{ g g}^{-1} \text{ hr}^{-1}$	Stanley and Naylor (1972)
MCMORT	Nonpredatory mortality rate			$0.001 \text{ g g}^{-1} \text{ hr}^{-1}$	Calibrated

(Continued)

(Sheet 1 of 5)

Table B1 (Continued)

Parameter	Description	Species	Value	Converted Value	Reference
TMPMAX	Maximum 7-day temperature change for non-predatory mortality			5°C	Boylen, unpublished data
T1	Critical low temperature for photosynthesis	<i>M. spicatum</i>	10°C	10°C	Van, Haller, and Boves (1976)
T1	Critical low temperature for photosynthesis	<i>H. verticillata</i>	10°C	10°C	Barko et al. (1980)
T2	Low optimum temperature for photosynthesis	<i>M. spicatum</i>	16°C	16°C	--
T2	Low optimum temperature for photosynthesis	<i>H. verticillata</i>	20°C	20°C	Barko et al. (1980)
T3	High optimum temperature for photosynthesis	<i>M. spicatum</i>	35°C	35°C	--
T3	High optimum temperature for photosynthesis	<i>H. verticillata</i>	24°C	24°C	Barko et al. (1980)
T4	Critical high temperature for photosynthesis	<i>M. spicatum</i>	44°C	44°C	Barko et al. (1980)
T4	Critical high temperature for photosynthesis	<i>H. verticillata</i>	32°C	32°C	Barko et al. (1980)

(Continued)

(Sheet 2 of 5)



Table B1 (Continued)

Parameter	Description	Species	Value	Converted Value	Reference
K1	Temperature rate multiplier for photosynthesis	<i>M. spicatum</i>	0.01	0.01	Calibrated
K1	Temperature rate multiplier for photosynthesis	<i>H. verticillata</i>	0.01	0.01	
K2		<i>M. spicatum</i>	0.98	0.98	
K2		<i>H. verticillata</i>	0.98	0.98	
K3		<i>M. spicatum</i>	0.98	0.98	
K3		<i>H. verticillata</i>	0.98	0.98	
K4		<i>M. spicatum</i>	0.28	0.28	
K4		<i>H. verticillata</i>	0.30	0.30	
T1	Critical low temperature for dark respiration	<i>M. spicatum</i>	5°C	5°C	
T1	Critical low temperature for dark respiration	<i>H. verticillata</i>	5°C	5°C	
T2	Low optimum temperature for dark respiration	<i>M. spicatum</i>	20°C	20°C	
T2	Low optimum temperature for dark respiration	<i>H. verticillata</i>	25°C	25°C	

(Continued)

Table B1 (Continued)

Parameter	Description	Species	Value	Converted Value	Reference
K1	Temperature multiplier for respiration	<i>M. spicatum</i>	0.01	0.01	Calibrated
K1		<i>H. verticillata</i>	0.01	0.01	
K2		<i>M. spicatum</i>	0.98	0.98	
K2		<i>H. verticillata</i>	0.98	0.98	
HTW	Average height-to-weight ratio	<i>M. spicatum</i>	1.27 m g <sup>-1</sup>	1.27 m g <sup>-1</sup>	Boylen, unpublished data
HTW	Average height-to-weight ratio	<i>H. verticillata</i>	0.416 m g <sup>-1</sup>	0.416 m g <sup>-1</sup>	Miller (1981)
O2FAC	Oxygen equivalent for macrophyte photosynthesis	<i>M. spicatum</i>	1.0	1.0	Brylinsky and Mann (1973)
O2RESP	Oxygen equivalent for macrophyte dark respiration	<i>M. spicatum</i>	1.2	1.2	Strickland (1960)
PLXGO(1)	Fraction of excreted matter released as PO <sub>4</sub> -P	<i>M. spicatum</i>	1 - 4%	0.01 - 0.04	Barko and Smart (1980)
PLXGO(1)	Fraction of excreted matter released as PO <sub>4</sub> -P	<i>H. verticillata</i>	7 - 29%	0.07 - 0.29	Barko and Smart (1980)

(Continued)

Table B1 (Concluded)

Parameter	Description	Species	Value	Converted Value	Reference
PLXGO(2)	Fraction of excreted matter released as $\text{NH}_4\text{-N}$		11%	0.11	Wetzel and Manny (1975)
PLXGO(3)	Fraction of excreted matter released as dissolved organic matter (DOM)		1 - 10%	0.01 - 0.10	Wetzel and Manny (1975)
PLDIGO(1)	Fraction of dead macrophyte that goes to DOM		1 - 10%	0.01 - 0.10	Wetzel and Manny (1975)
PLDIGO(2)	Fraction of dead macrophyte that goes to detritus		29%	0.29	Godshalk and Wetzel (1978)
PLDIGO(3)	Fraction of dead macrophyte that goes to sediment		18%	0.18	Carpenter (1976)

DATE  
FILMED  
-8